

Evidence for Single Top Quark Production at DØ & A First Direct Measurement of $|V_{tb}|$

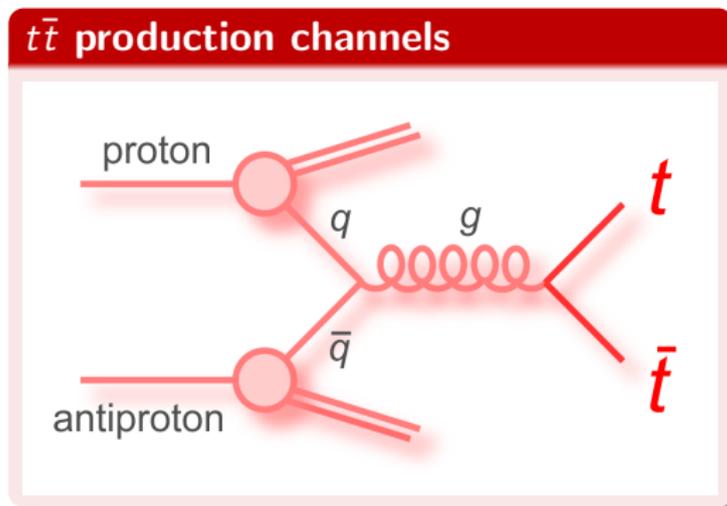
Dag Gillberg
For the DØ Collaboration



SIMON FRASER
UNIVERSITY

The Top Quark

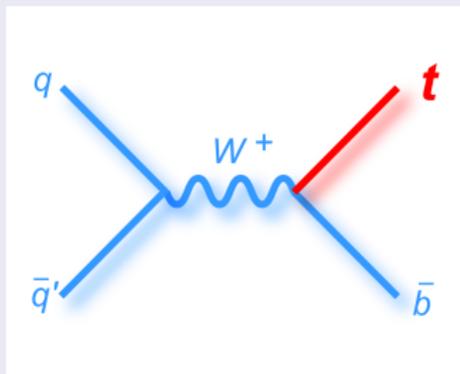
- Top pair ($t\bar{t}$) production observed 1995 by the DØ and the CDF Collaborations
- By far the heaviest fundamental particle we know of
- Cross section: 6.8 ± 0.6 pb (incl. uncert. on the mass $\rightarrow \pm 1.2$ pb)



Electroweak single top production

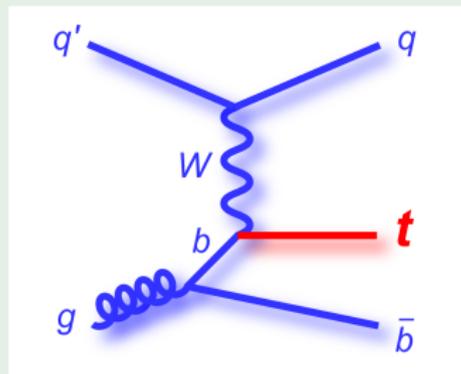
- Never observed before
- Dominant production channels at the Tevatron:

s-channel (tb)



$$\sigma_{\text{NLO}} = 0.88 \pm 0.11 \text{ pb (*)}$$

t-channel (tqb)



$$\sigma_{\text{NLO}} = 1.98 \pm 0.25 \text{ pb(*)}$$

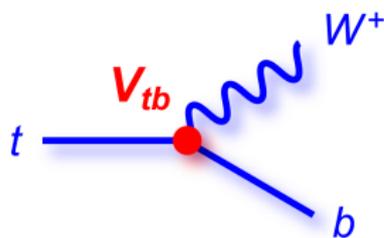
(*) $m_t = 175 \text{ GeV}$, Phys.Rev. D70 (2004) 114012

- Total SM cross section: $\sigma_{s+t} = 2.9 \text{ pb}$

Motivation

1. Predicted but not observed before
2. **Study the Wtb coupling**

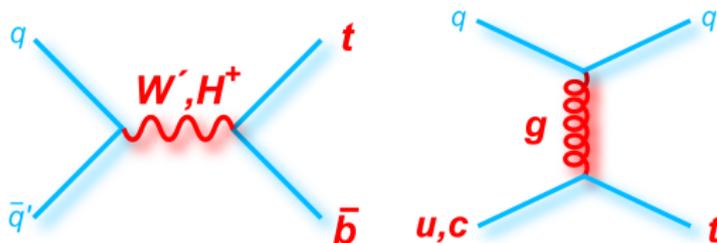
$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



- Direct measurement of $|V_{tb}|$ (more later)
 - Unitarity test of CKM matrix
 - Anomalous Wtb couplings
3. Measurement of top quark properties:
polarization, decay width, lifetime, mass...

4. New physics, example:

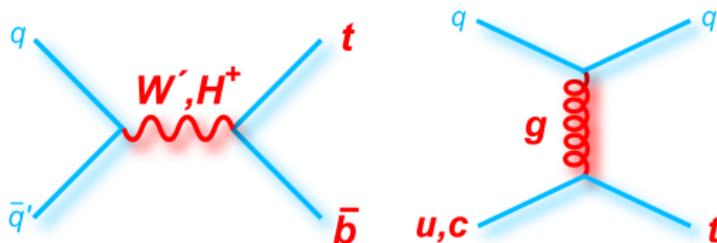
- s -channel: resonances like heavy W' , charged Higgs
- t -channel: Flavour-changing neutral currents
- 4-th quark generation?



Motivation

4. New physics, example:

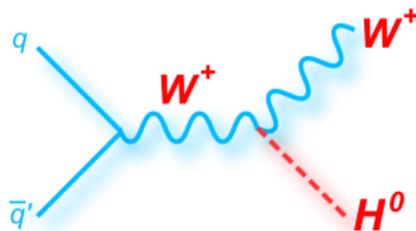
- s -channel: resonances like heavy W' , charged Higgs
- t -channel: Flavour-changing neutral currents
- 4-th quark generation?



5. Very similar to SM Higgs production

- Same final state and bkg as

$$WH \rightarrow l\nu b\bar{b}$$



6. Test of advanced separation techniques

Signal and backgrounds samples

Single top signal, MC

- COMPHEP-SINGLETOP

W+jets, MC

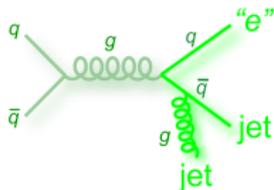
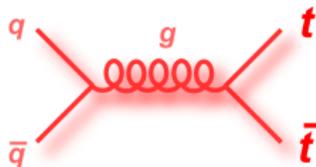
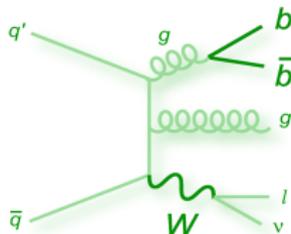
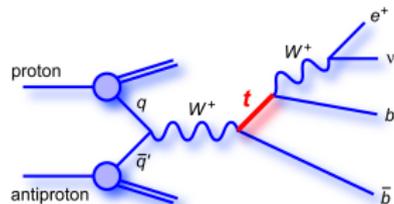
- Most difficult background
- Shapes from ALPGEN
- Normalization and heavy flavour fraction from data

t \bar{t} , MC

- ALPGEN
- Normalized to $\sigma_{NNLO} = 6.8$ pb

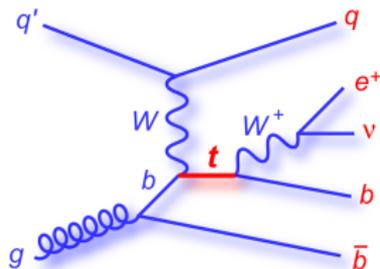
Multijet events, from data

- misidentified lepton



Analysis Strategy

Strategy: Maximize signal acceptance – extract signal using multivariate techniques

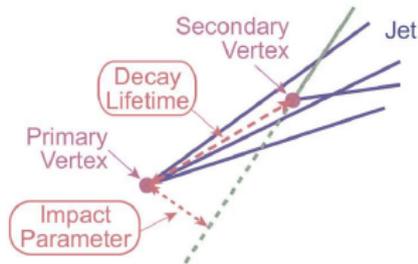


Signature

- isolated lepton
- \cancel{E}_T (from ν)
- jets
- at least 1 b -jet

Event selection

- One lepton:
 - electron: $p_T > 15$ GeV, $|\eta_{det}| < 1.1$
 - muon: $p_T > 18$ GeV, $|\eta_{det}| < 2$
- $\cancel{E}_T > 15$ GeV
- 2-4 jets: $p_T > 15$ GeV, $|\eta| < 3.4$
 - Leading jet: $p_T > 25$ GeV, $|\eta_{det}| < 2.5$
 - Second leading jet: $p_T > 20$ GeV
- 1-2 jets b -tagged



b -tagging

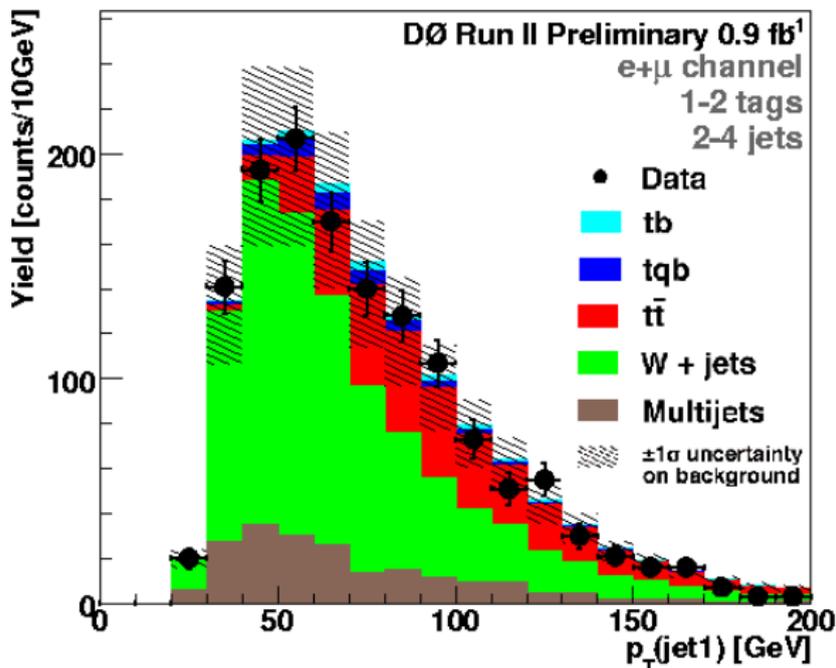
Data-background model agreement

Expected N_{events}

$s + t$ signal	62
$t\bar{t}$	348
W_{jj}	174
W_{bb} & W_{cc}	675
multijet	201

data/bkg N_{events}

signal	62
background	1399
data	1398



*We have hundreds of these kind of plots
for other kinematic variables*

The 12 (l_{ep}, N_{tag}, N_{jet})-bins

W Transverse Mass

Electrons

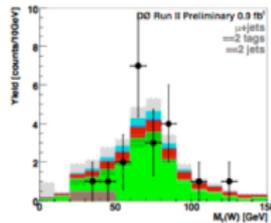
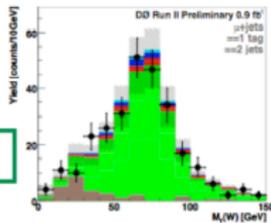
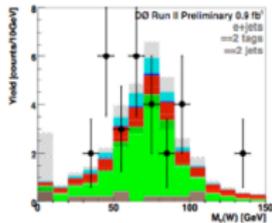
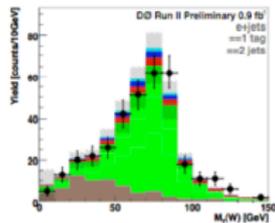
Muons

1 tag

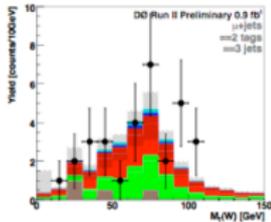
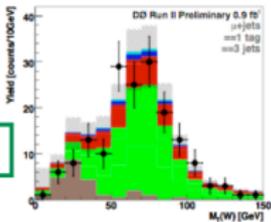
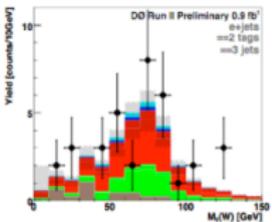
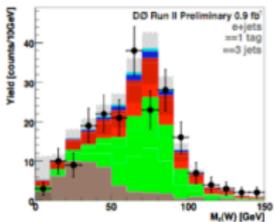
2 tags

1 tag

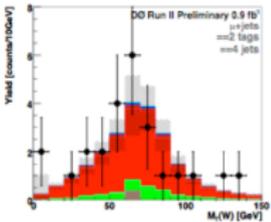
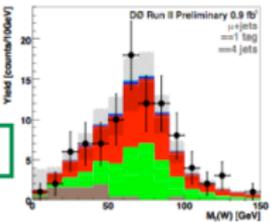
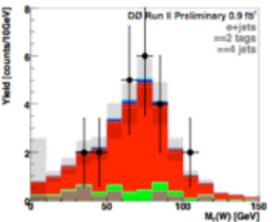
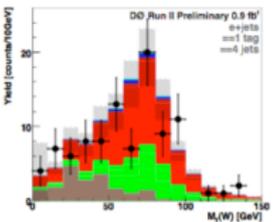
2 tags



2 jets



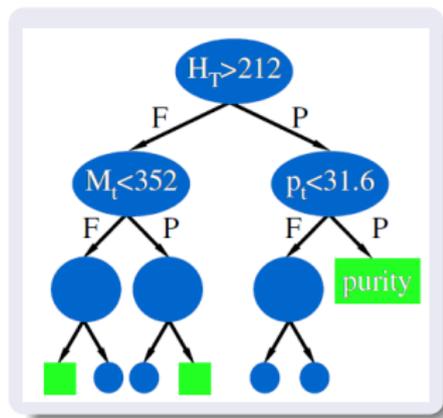
3 jets



4 jets

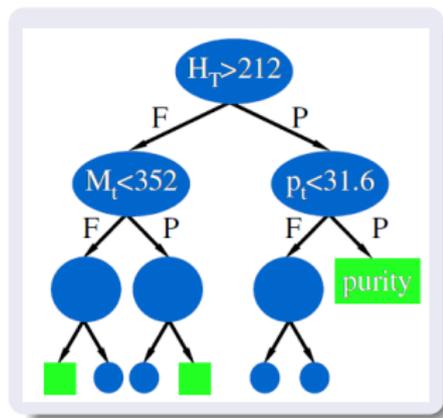
The Decision Tree Analysis

- Single top signal sample trained against our background samples
- Idea: recover events that fail criteria in cut-based analysis
- Separate training per $(l_{ep}, N_{tag}, N_{jet})$ -bin
- **Boosting** – give mis-classified events higher weight and re-train! (20 times)



The Decision Tree Analysis

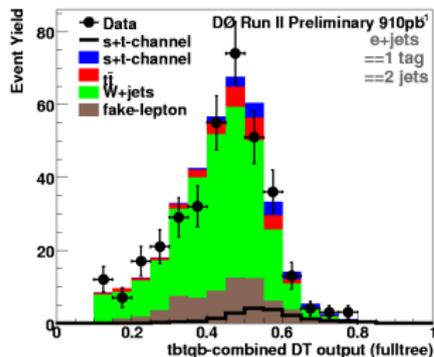
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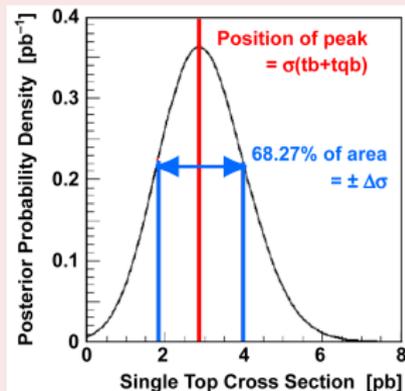
Discriminating variables

- 49 variables used, categories:
object kinematics, global event kinematics, angular correlations
- Most discriminating power:
 $m(\text{alljets}), m(W, b\text{-jet1}), \cos(b\text{-jet1}, l_{ep}), q_{lep} \times \eta_{\text{un-tagged jet1}}$

The Decision Tree Analysis



Decision Tree Output



Bayesian posterior

- Bayesian posterior probability density:

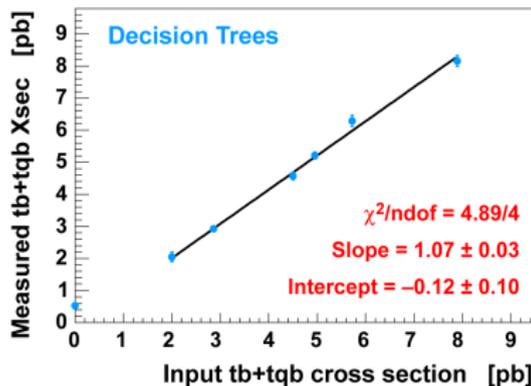
$$P(\sigma|D) \int_{a,b} P(D|\sigma, a, b) \text{Prior}(\sigma) \text{Prior}(a, b)$$

- Shape and normalization systematics treated as nuisance parameters
- Correlations between uncertainties properly accounted for

Ensemble Testing

Tested our machinery with many sets of **pseudo-data**

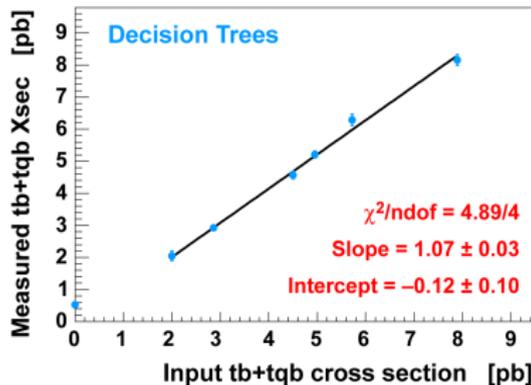
- Subset of our total pool of background events
- Individual statistical and systematical fluctuations
- **Wonderful tool** – like running DØ 1000s of times!
- Generated several ensembles with different single top content →



Ensemble Testing

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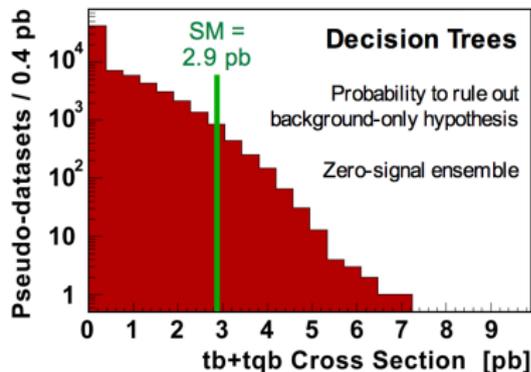
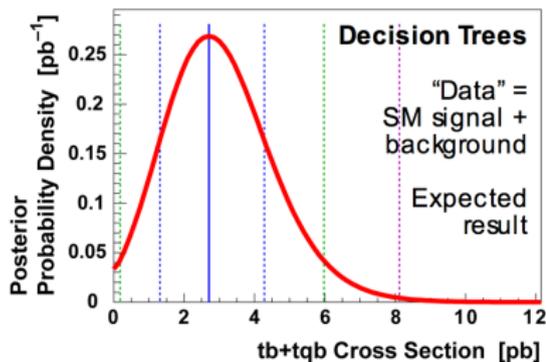


Significance

- Used 70,000 pseudo-datasets with **no single top content**
- We measure the fraction of zero-signal datasets in which we derive at least the SM cross section (**expected significance**), or at least the observed cross section (**observed significance**)

Expected Decision Tree Results

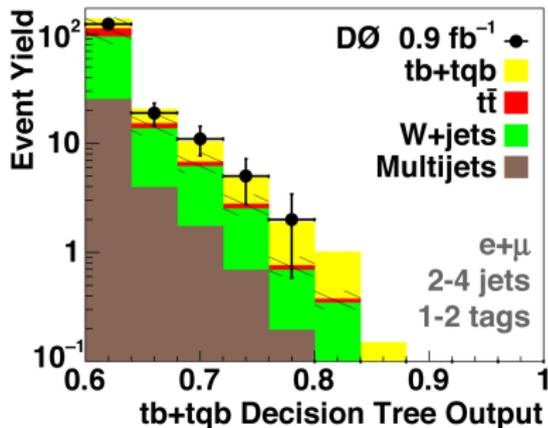
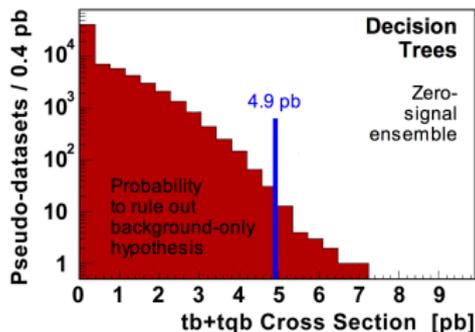
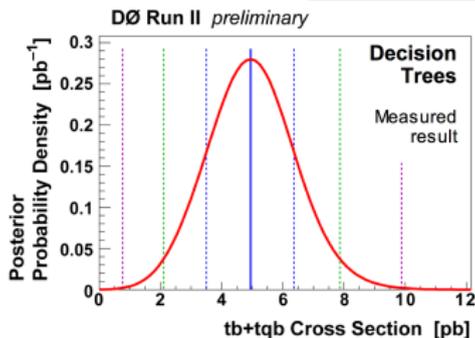
Expected cross section	$2.7^{+1.5}_{-1.4}$ pb
Expected p-value	1.9%
Expected significance	2.1σ



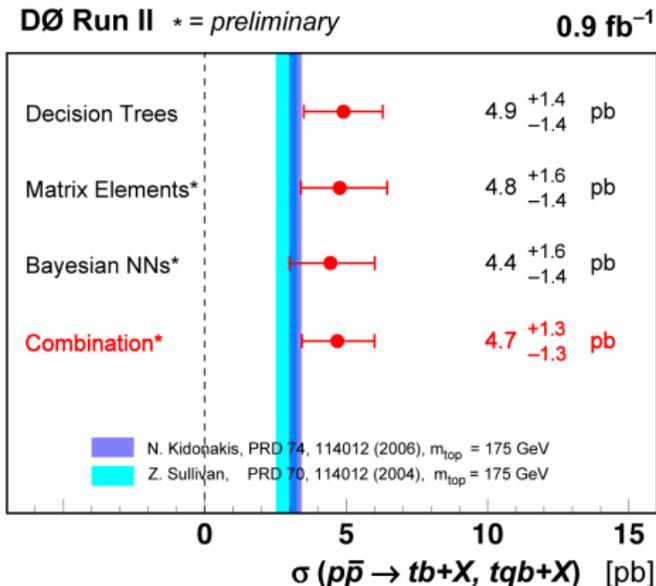
Boosted decision tree observed results

$\sigma_{s+t} = 4.9 \pm 1.4 \text{ pb}$
 $p\text{-value} = 0.035\% (3.4\sigma)$
SM compatibility: 11% (1.3σ)

Evidence!



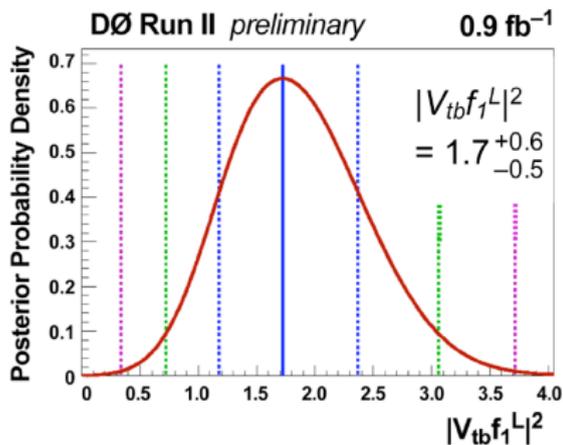
Observed σ_{s+t} for all three analyses



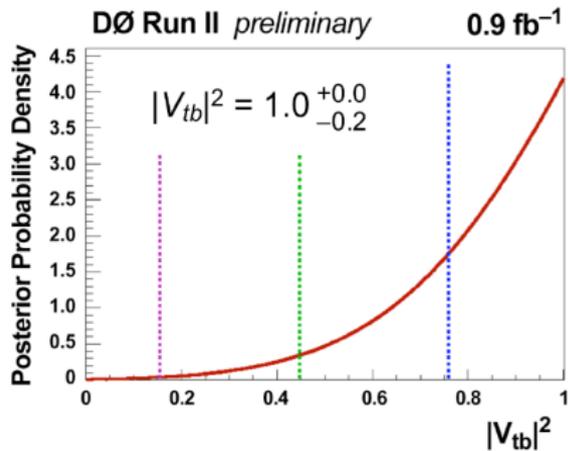
- The three analyses give consistent results!
- **Combined result using the BLUE method:**
 4.7 ± 1.3 pb with **3.6σ** significance!
- Same data used (0.9 fb^{-1}) – therefore correlated

First direct measurement of $|V_{tb}|$

- Assuming $V_{td}^2 + V_{ts}^2 \ll V_{tb}^2$ and pure $V-A$ and CP-conserving Wtb interaction



$$|V_{tb} f_1^L| = 1.3 \pm 0.2$$



$$0.68 < |V_{tb}| \leq 1 \text{ @ 95\% CL}$$

(assuming $f_1^L = 1$,
flat prior in $[0, 1]$)

- No assumption about number of quark families or CKM unitarity

Boosted Decision Trees result published: PRL 98, 181802

First evidence for single top production found at DØ!

$$\sigma(p\bar{p} \rightarrow tb + X, tqb + X) = 4.9 \pm 1.4 \text{ pb}$$

3.4 σ significance

First direct measurement of $|V_{tb}|$

$$|V_{tb}f_1^L| = 1.3 \pm 0.2$$

assuming $f_1^L = 1$ (SM): $0.68 < |V_{tb}| \leq 1$ @ 95% CL

Latest result:

Combined result, DT + New ME + New BNN

$$\sigma(p\bar{p} \rightarrow tb + X, tqb + X) = 4.7 \pm 1.3 \text{ pb}$$

3.6 σ significance

BACKUP SLIDES

Systematics Uncertainties

Source of Uncertainty	Size
Top pairs normalization	18%
W+jets & multijets normalization	18–28%
Integrated luminosity	6%
Trigger modeling	3–6%
Lepton ID corrections	2–7%
Jet modeling	2–7%
Other small components	Few %
Jet energy scale	1–20%
Tag rate functions	2–16%

Expected signal yields and S:B ratios

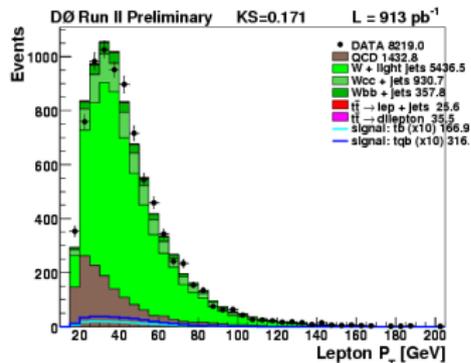
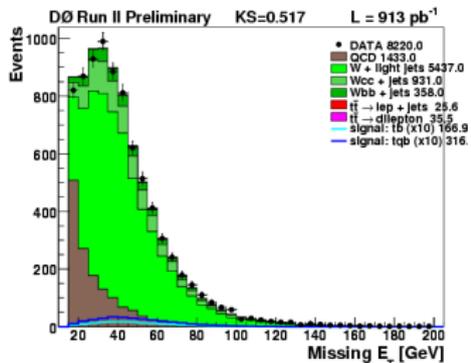
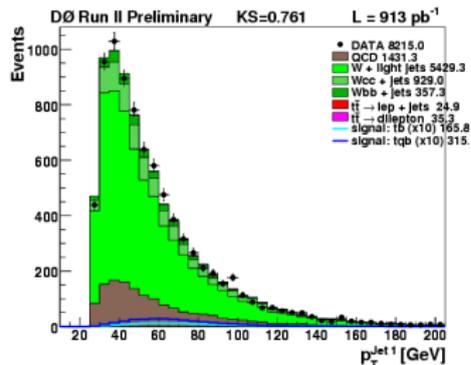
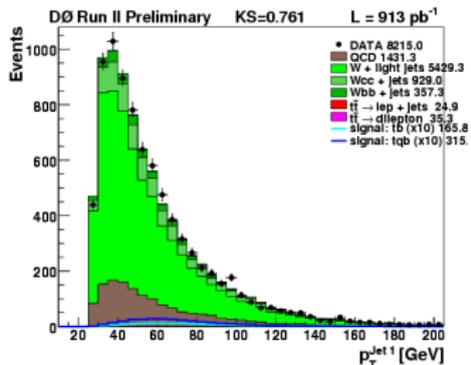
Percentage of single top *tb+tb* selected events and S:B ratio (white squares = no plans to analyze)

Electron + Muon	1 jet	2 jets	3 jets	4 jets	≥ 5 jets
0 tags	10% 1 : 3,200	25% 1 : 390	12% 1 : 300	3% 1 : 270	1% 1 : 230
1 tag	6% 1 : 100	21% 1 : 20	11% 1 : 25	3% 1 : 40	1% 1 : 53
2 tags		3% 1 : 11	2% 1 : 15	1% 1 : 38	0% 1 : 43

Yields before b -tagging

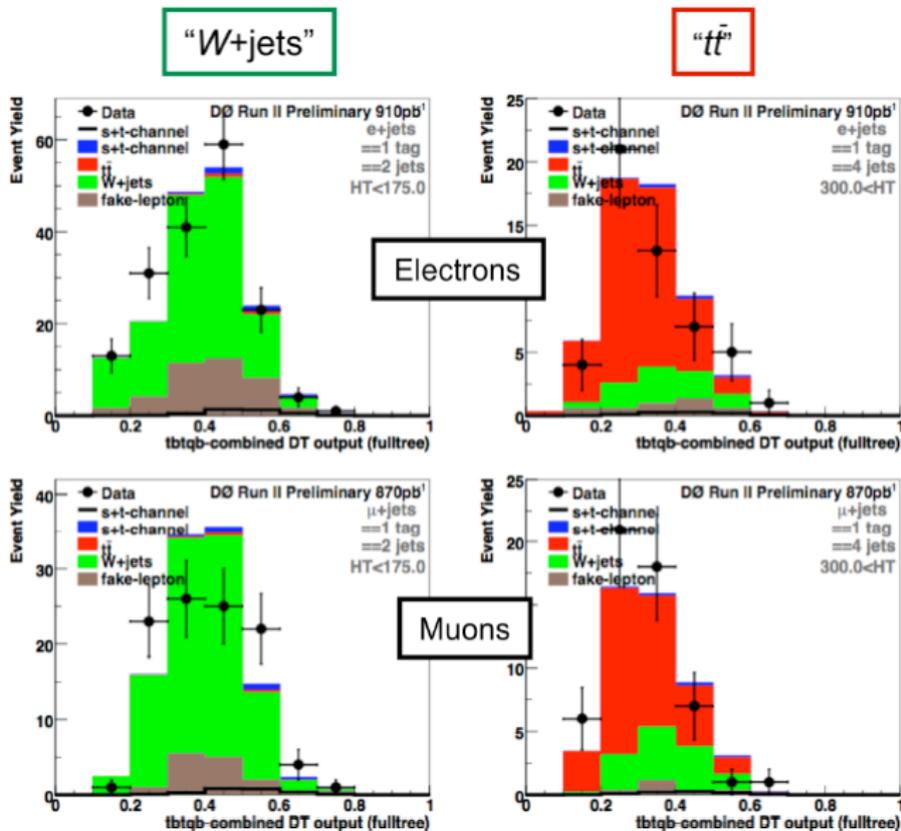
Source	Event Yields in 0.9 fb^{-1} Data		
	Electron+muon combined, before b -tagging		
	2 jets	3 jets	4 jets
tb	25	12	3
tqb	47	25	8
$t\bar{t} \rightarrow ll$	62	50	18
$t\bar{t} \rightarrow l+\text{jets}$	40	175	227
$W+b\bar{b}$	670	310	89
$W+c\bar{c}$	1,959	912	224
$W+jj$	10,160	3,138	728
Multijets	1,762	1,083	314
Total background	14,654	5,667	1,601
Data	14,652	5,665	1,601

Data-background agreement before b -tagging

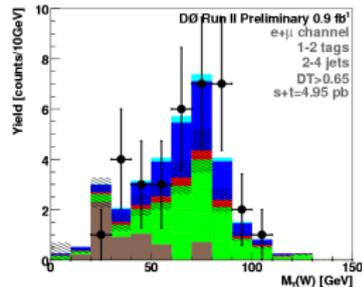
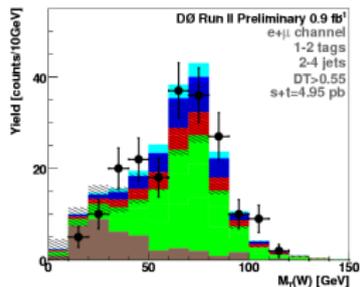
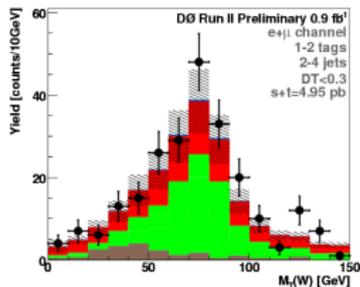
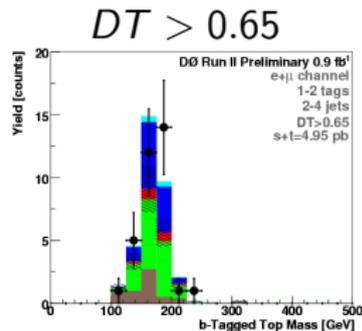
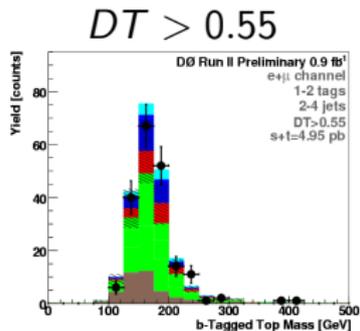
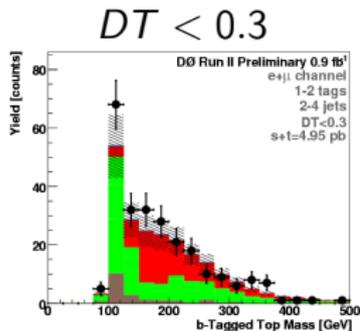


• Background model show good agreement with data!

Cross-check samples



Boosted decision tree event characteristics



Decision Trees - 49 input variables

Object Kinematics

$p_T(\text{jet1})$
 $p_T(\text{jet2})$
 $p_T(\text{jet3})$
 $p_T(\text{jet4})$
 $p_T(\text{best1})$
 $p_T(\text{notbest1})$
 $p_T(\text{notbest2})$
 $p_T(\text{tag1})$
 $p_T(\text{untag1})$
 $p_T(\text{untag2})$

Angular Correlations

$\Delta R(\text{jet1}, \text{jet2})$
 $\cos(\text{best1}, \text{lepton})_{\text{besttop}}$
 $\cos(\text{best1}, \text{notbest1})_{\text{besttop}}$
 $\cos(\text{tag1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{tag1}, \text{lepton})_{\text{btaggedtop}}$
 $\cos(\text{jet1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{jet1}, \text{lepton})_{\text{btaggedtop}}$
 $\cos(\text{jet2}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{jet2}, \text{lepton})_{\text{btaggedtop}}$
 $\cos(\text{lepton}, Q(\text{lepton}) \times z)_{\text{besttop}}$
 $\cos(\text{lepton}_{\text{besttop}}, \text{besttop}_{\text{CMframe}})$
 $\cos(\text{lepton}_{\text{btaggedtop}}, \text{btaggedtop}_{\text{CMframe}})$
 $\cos(\text{notbest}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{notbest}, \text{lepton})_{\text{besttop}}$
 $\cos(\text{untag1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{untag1}, \text{lepton})_{\text{btaggedtop}}$

Event Kinematics

Aplanarity(alljets, W)
 $M(W, \text{best1})$ ("best" top mass)
 $M(W, \text{tag1})$ ("b-tagged" top mass)
 $H_T(\text{alljets})$
 $H_T(\text{alljets} - \text{best1})$
 $H_T(\text{alljets} - \text{tag1})$
 $H_T(\text{alljets}, W)$
 $H_T(\text{jet1}, \text{jet2})$
 $H_T(\text{jet1}, \text{jet2}, W)$
 $M(\text{alljets})$
 $M(\text{alljets} - \text{best1})$
 $M(\text{alljets} - \text{tag1})$
 $M(\text{jet1}, \text{jet2})$
 $M(\text{jet1}, \text{jet2}, W)$
 $M_T(\text{jet1}, \text{jet2})$
 $M_T(W)$
Missing E_T
 $p_T(\text{alljets} - \text{best1})$
 $p_T(\text{alljets} - \text{tag1})$
 $p_T(\text{jet1}, \text{jet2})$
 $Q(\text{lepton}) \times \eta(\text{untag1})$
 \sqrt{s}
Sphericity(alljets, W)

- Adding variables does not degrade performance
- Tested shorter lists, lost some sensitivity
- Same list used for all channels

Sensitivity determination

Using 70,000 pseudo-datasets without any single top content:

Expected p-value

Fraction of 0-signal pseudo-datasets in which we measure at least 2.9 pb (SM σ)

Observed p-value

Fraction of 0-signal pseudo-datasets in which we measure at least the observed cross section

Measuring a cross section

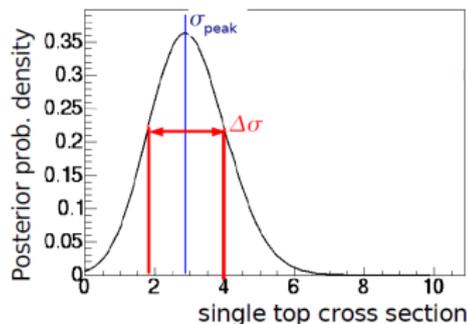
Probability to observe data distribution D , expecting y :

$$y = \alpha l \sigma + \sum_{s=1}^N b_s \equiv a \sigma + \sum_{s=1}^N b_s$$

$$P(D|y) \equiv P(D|\sigma, a, b) = \prod_{i=1}^{nbins} P(D_i|y_i)$$

The cross section is obtained

$$Post(\sigma|D) \equiv P(\sigma|D) \propto \int_a \int_b P(D|\sigma, a, b) Prior(\sigma) Prior(a, b)$$



- Bayesian posterior probability density
- Shape and normalization systematics treated as nuisance parameters
- Correlations between uncertainties properly accounted for
- Flat prior in signal cross section

First direct measurement of $|V_{tb}|$

- General form of Wtb vertex:

$$\Gamma_{Wtb}^\mu = -\frac{g}{\sqrt{2}} V_{tb} \left\{ \gamma^\mu [f_1^L P_L + f_1^R P_R] - \frac{i\sigma^{\mu\nu}}{M_W} (p_t - p_b)_\nu [f_2^L P_L + f_2^R P_R] \right\}$$

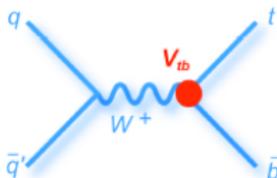
- Assume

- SM top quark decay : $V_{td}^2 + V_{ts}^2 \ll V_{tb}^2$
- Pure V-A : $f_1^R = 0$
- CP conservation : $f_2^L = f_2^R = 0$

- No need to assume only three quark families or CKM matrix unitarity

(unlike for previous measurements using $t\bar{t}$ decays)

- Measure the strength of the V-A coupling, $|V_{tb} f_1^L|$, which can be > 1



Additional theoretical uncertainties

	tb	tqb
Top mass	13 %	8.5 %
Scale	5.4 %	4.0 %
PDF	4.3 %	10 %
α_s	1.4 %	0.01 %